An overview of ExaConstit and its use in the ExaAM project

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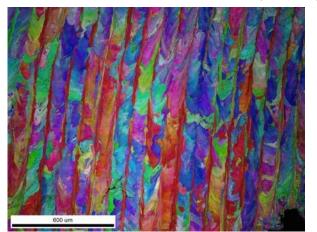
Outline

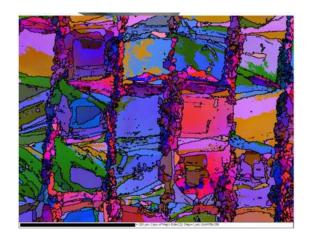
- Motivation and overview of project
- Overview of ExaConstit
 - FEM formulation
- Overview of GPU Porting Efforts
 - Element assembly formulation
 - Exascale readiness of ExaConstit
- Overview of local property calculation workflow
- ExaConstit's use in other areas
- Conclusion/On-going work

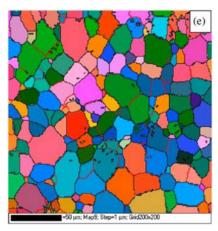


Motivation

- AM produces as-built metals that are characteristically quite different from typical manufacturing processes in both the microstructure and mechanical response [2]
- Want to couple the microstructure development and the local macroscopic properties
 - Can be accomplished through crystal plasticity models that utilize finite elements



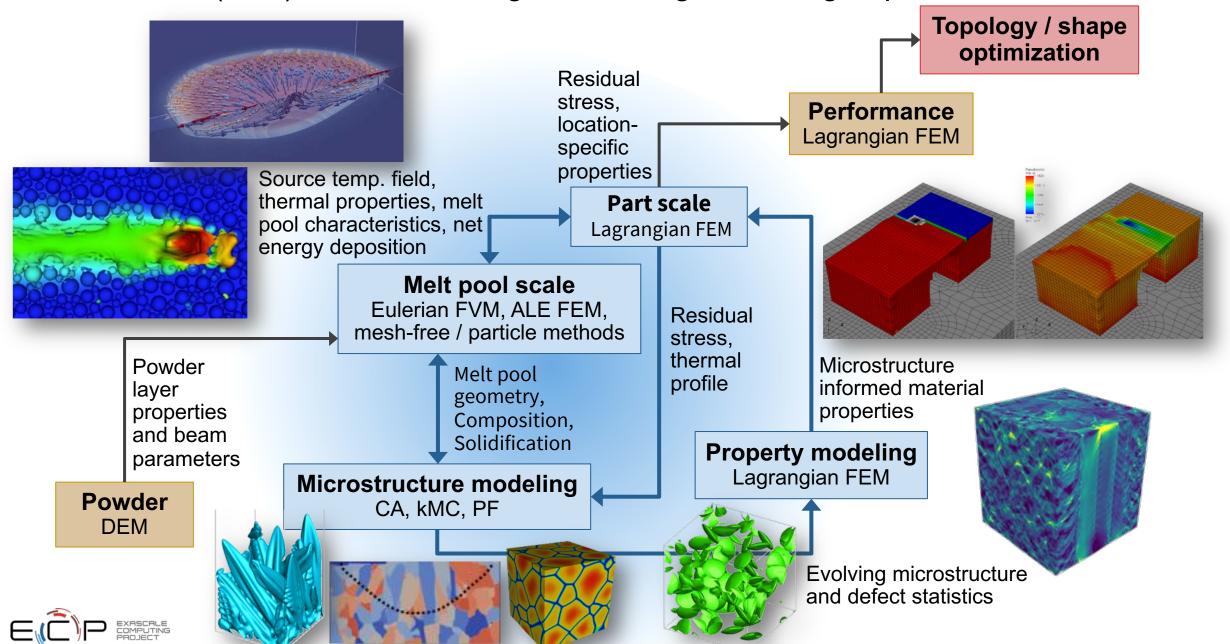




Microstructure of an AM part at 2 different locations (Left and Middle) [3] and a traditional manufacturing microstructure [4]



ExaAM focus (blue) fits within a larger modeling and design optimization context



A full ExaAM simulation consists of five stages

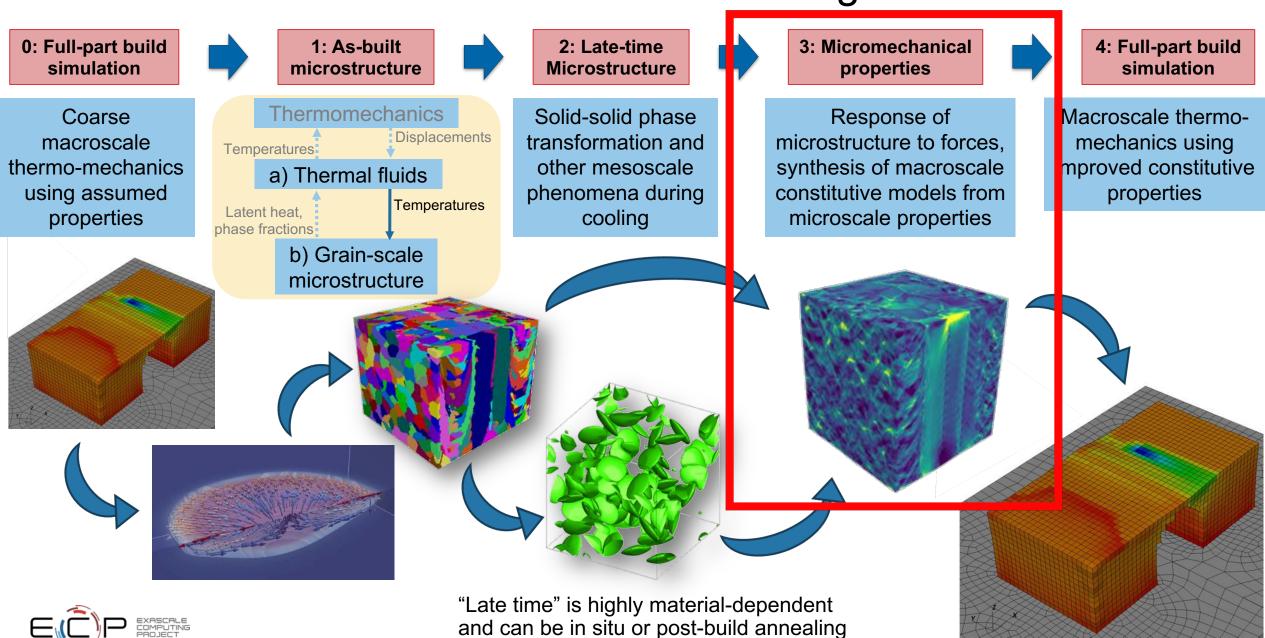
3: Micromechanical 0: Full-part build 1: As-built 2: Late-time 4: Full-part build simulation microstructure **Microstructure** properties Thermomechanics Macroscale thermo-Coarse Solid-solid phase Response of Displacements transformation and macroscale microstructure to forces. mechanics using Temperatures thermo-mechanics improved constitutive other mesoscale synthesis of macroscale a) Thermal fluids constitutive models from phenomena during properties using assumed Temperatures Latent heat. properties microscale properties cooling phase fractions b) Grain-scale microstructure

> "Late time" is highly material-dependent and can be in situ or post-build annealing



simulation

A full ExaAM simulation consists of five stages



Overview of ExaConstit

- A new nonlinear quasi-static, implicit FEM solid mechanics code built on the MFEM library
 - Development began in 2018 for ExaAM project
 - Updated Lagrangian formulation (velocity based)
 - Natively supports a wide range of element types
 - Supports complex parts and non-trivial/changing Dirichlet BCs
 - Available at https://github.com/LLNL/ExaConstit



Overview of ExaConstit

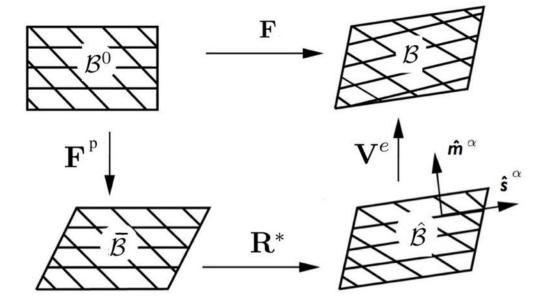
- Designed with exascale computers in mind but performant even on desktop machines
- New features, workflows, and post-processing tools are constantly being added
- Bread and butter is crystal plasticity type problems
 - Crystal plasticity models are provided through ExaCMech library
 - ExaCMech is available at https://github.com/LLNL/ExaCMech
 - Models can be upwards of 75-90x faster than Abaqus UMAT runs
 - Users can also run UMAT problems as well
 - UMAT framework enables us to run a wide range of industry and research models



Model Overview

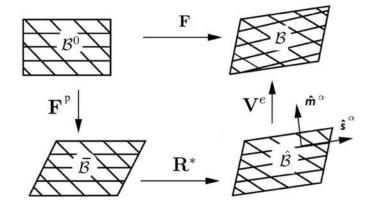
- A large strain single crystal elasto-viscoplastic model is being used
 - Small deviatoric elastic strain assumption is made

$$\mathbf{F} = \mathbf{F}^e \mathbf{F}^p$$





Model Overview



$$\mathbf{L} = \dot{\mathbf{V}}^e \mathbf{V}^{e-1} + \mathbf{V}^e \hat{\mathbf{L}}^p \mathbf{V}^{e-1}$$

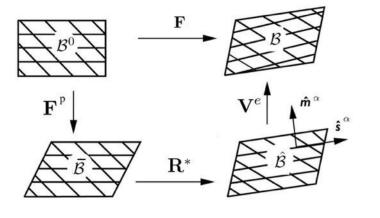
$$\hat{\mathbf{L}}^{p} = \dot{\mathbf{R}}^{*} \mathbf{R}^{*T} + \mathbf{R}^{*} \dot{\mathbf{F}}^{p} \mathbf{F}^{p-1} \mathbf{R}^{*T}$$

$$\bar{\mathbf{L}}^{p} = \dot{\mathbf{F}}^{p} \mathbf{F}^{p-1} \qquad \bar{\mathbf{L}}^{p} = \sum_{\alpha=1}^{n} \dot{\gamma}^{\alpha} \bar{\mathbf{s}}^{\alpha} \otimes \bar{\mathbf{m}}^{\alpha}$$

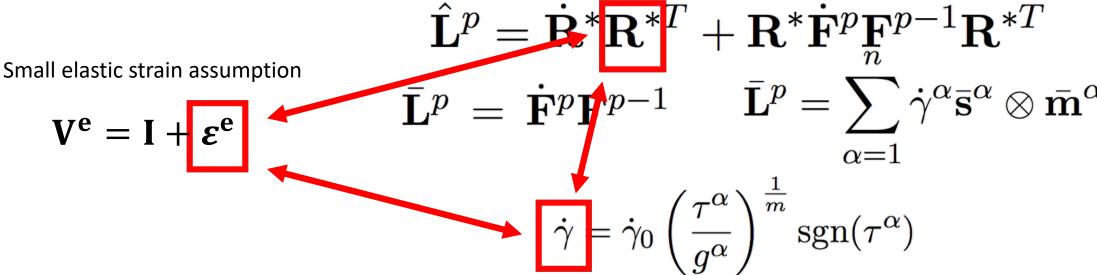
$$\dot{\gamma} = \dot{\gamma}_{0} \left(\frac{\tau^{\alpha}}{g^{\alpha}} \right)^{\frac{1}{m}} \operatorname{sgn}(\tau^{\alpha})$$



Model Overview



$$\mathbf{L} = \dot{\mathbf{V}}^e \mathbf{V}^{e-1} + \mathbf{V}^e \hat{\mathbf{L}}^p \mathbf{V}^{e-1}$$





FEM Formulation

- We're solving for the conservation of linear momentum using a Newton Raphson scheme
 - Our finite element formulation takes on a form very similar to linear elasticity
 - We make use of an updated Lagrangian formulation here

$$[K_{tan}]\{-\Delta \mathbf{V}\} = \{f_{int}\}\$$

$$[K_{tan}] = \int_{\Omega} [\mathbf{B}]^{\mathrm{T}} [\boldsymbol{C}^{\boldsymbol{\sigma} \boldsymbol{\tau}}] [\mathbf{B}] d\Omega \qquad [\boldsymbol{C}^{\boldsymbol{\sigma} \boldsymbol{\tau}}] = \frac{\mathrm{d} \boldsymbol{\sigma}}{\mathrm{d} \boldsymbol{d}}$$

$$\{f_{int}\} = \int_{\Omega} [\mathbf{B}]^{\mathrm{T}} \{\boldsymbol{\sigma}\} d\Omega$$

$$\{\mathbf{V}\}^{i+1} = \{\mathbf{V}\}^i + \{\Delta\mathbf{V}\}$$

$$\{\mathbf{x}\}^{t+\Delta t} = \{\mathbf{x}\}^t + \Delta t \{\mathbf{V}\}^{i+1}$$

Note: This formulation uses the velocity rather than the typical displacement



Transitioning over to the GPU: Separate Material Model and FEM code

- ExaConstit originally had the material model calculation tied in with the linearized RHS calculation and compute stiffness matrix
 - This strategy does not scale well as different assembly operations are added
- Refactored code into a set-up phase, pre-processing step before assembly, RHS calculations, and gradient calculation / operation



Set-up phase

- Calculate necessary parameters to use within our material model
 - Pre-processing stage for material kernel
- Material kernel stage
- Post-processing material kernel stage
 - Perform what-ever steps are necessary for material kernel's data to be used by the rest of the code
- MFEM_FORALL loops are used for pre & post processing steps
- Material model uses its own parallelization strategy



An Element Assembly Formulation

- We're making use of efficient formulations developed back in the 80s [5]
- $\{f_{int}\}\$ is just calculated using partial assembly formulation
- This formulation allows us an efficient way to compute sub-blocks of $[K_{tan}]$
 - Could further specialize this for tensor-type elements for further performance gains

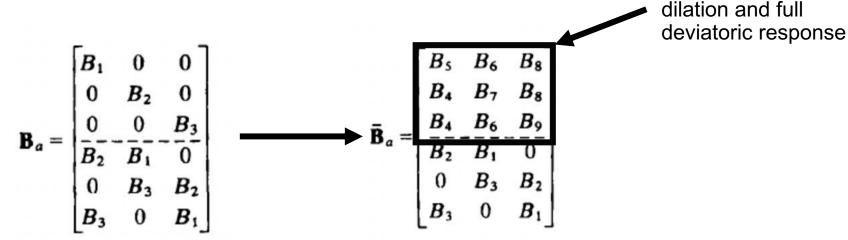
$$[K_{tan}] = \int_{\Omega} [\mathbf{B}]^{\mathrm{T}} [\mathbf{C}^{\sigma \tau}] [\mathbf{B}] d\Omega$$
$$[K_{tan}] = \int_{\Omega} [\mathbf{b_1} \mathbf{b_2} \dots \mathbf{b_N}]^T [\mathbf{C}^{\sigma \tau}] [\mathbf{b_1} \mathbf{b_2} \dots \mathbf{b_N}] d\Omega$$
$$[\mathbf{b_1} \mathbf{b_2} \dots \mathbf{b_N}] = [\mathbf{B}]$$

$$\{f_{int}\} = \int_{\Omega} [\mathbf{B}]^{\mathrm{T}} \{\boldsymbol{\sigma}\} d\Omega$$
$$\det(J) w_{qpt} \nabla_{ij} \phi_{\xi}^{T} J_{jk}^{-T} \sigma_{kl}$$



Incompressible Material Support within ExaConstit

- An initial integration formulation for incompressible has been implemented
 - Based on the work presented in [6]
 - New integrators are not as simple to port over to the element assembly formulation
- This formulation brings linear hexahedron response much more in line with response from higher order elements
 - Runtime is comparable to full integration approach



Full integration gradient matrix

Incompressible integration gradient matrix

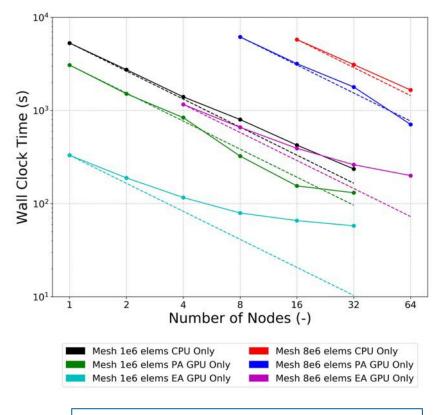
Contains a mean



Exascale Readiness Status: ExaConstit

Summit performance

- 15x speed-up with GPU implementation over CPU
- GPU strong and weak scaling for most performant assembly method (element assembly)
- Poor strong and weak scaling is due to start-up cost of reading in the mesh and partitioning it
 - Recent work-in-progress within MFEM is expected to drastically improve this area (Thanks Veselin!)
- Ported ExaCMech over to HIP this past year
 - ExaConstit port will follow this year



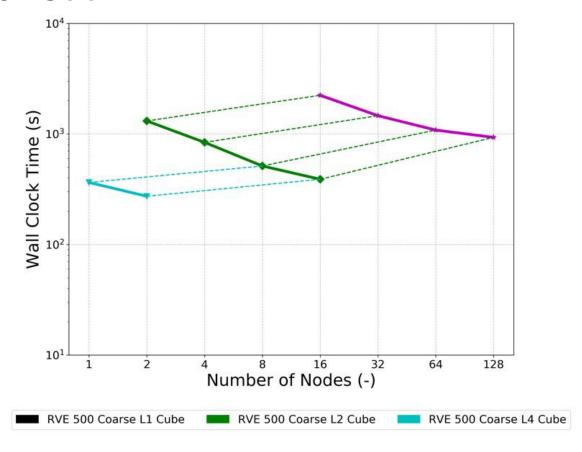
Strong scaling across different assembly methods



Exascale Readiness Status: ExaConstit

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Strong and weak scaling of a typical AM microstructure



Computational shifts between GPU and Host Runs

Summit performance

- How do computational costs shift when moving from CPU to GPU?
 - Looking at a 450k element mesh run with Caliper
- Krylov solver still dominates run time
- What's going on with the MPI calls?
 - MPI is taking up a larger % of our runtime now
 - Partially due to issues with MPI D2D calls not being as performant as possible
 - MPI times are 40% less on the GPU though
- Improvements could be made by looking at communication hiding Krylov solvers

CPU Kernel Name	Time % (total)
Krylov Solver	84.534
Material Model	7.091
MPI Calls	6.778
Element Assembly	0.577
Simulation Initialization	0.295
Material Model Setup	0.283
Integrator Setup	0.137
Total	99.69

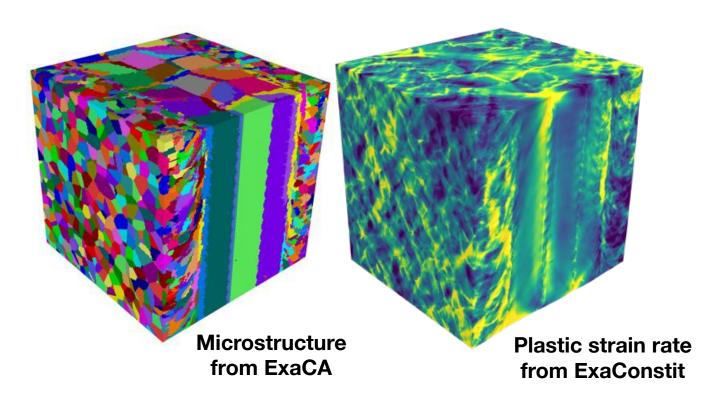
GPU Kernel Name	Time % (total)
Krylov Solver	55.16
MPI Calls	18.83
Element Assembly	15.80
Material Model	6.28
Simulation Initialization	1.39
Integrator Setup	0.93
Main Driver	0.88
Assemble Diagonal	0.47
Post-processing step	0.14
Total	99.87



Stage 3: Micromechanical properties (ExaConstit)

- We now have a performant code but what do we need that for?
- ExaAM requires local property to be calculated from microstructures obtained through out an AM part
- Local properties are calculated by running tons of crystal plasticity simulations under varying loading conditions and temperatures
 - Simply running 1 simulation per microstructure is not adequate for AM parts
 - Complex macroscopic models are needed for part scale simulations (not computed by ExaConstit)

AMB2018-01 L8 microstructure generated by ExaCA 0.5³ mm domain, 3475 grains

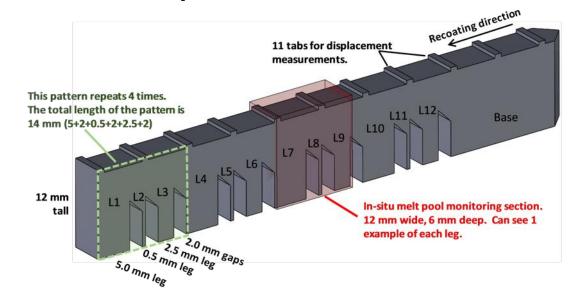


- Localization of plastic strain is non-trivial for these complex AM microstructures What is an appropriate RVE?
- Hydrostatic stress is commonly used to drive porosity models - How can we appropriately homogenize?

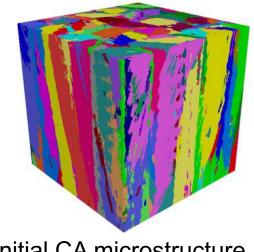


Representative Volume Element for Macroscopic Calculations

- Microstructure was obtained from a cellular automata simulation based on scan paths of the NIST AM benchmark problem AMB2018-01. Thermal histories provided by either TruchasPBF or OpenFOAM simulations of the scan path
 - Inconel 625 material
 - Voce hardening model parameterized against AFRL MIDAS challenge 3 data [7]
 - Scan pattern mimics one of the larger legs of the AMB2018-01
 - Microstructure used is away from edge boundaries
 - 500³ microns sample with 300³ voxel size



AMB2018-01 part

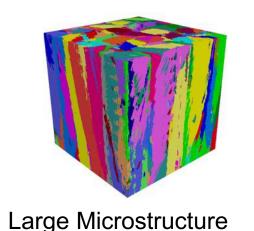


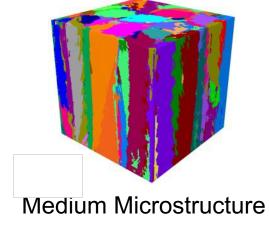


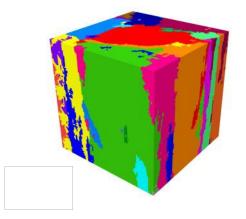


Domain Size Microstructures

- Microstructures are all taken from the middle of the initial 500³ microns sample
- Microstructures have dimensions: 500³ microns, 333.3³ microns, and 166.7³ microns
 - 27, 8, and 1 million linear hexahedron elements respectively
- Uniaxial tension tests out to 5% were taken on these samples
 - Symmetry boundary conditions were applied to all samples
 - Large strains are not of great interest to our AM applications





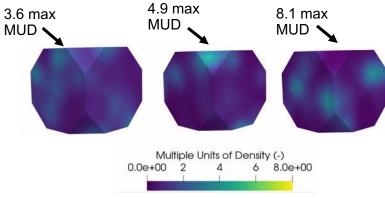


Small Microstructure

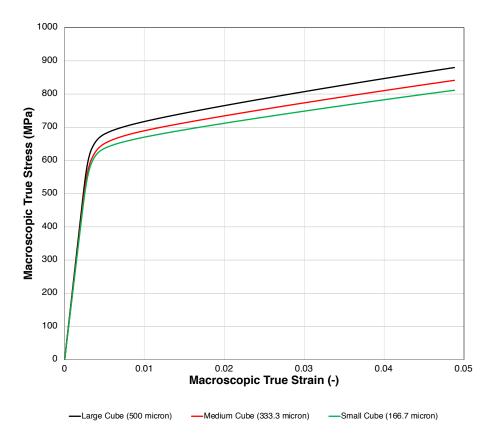


Macroscopic Stress Strain Response

- The medium cube was below 5% error for the entire loading history
 - Error continues to grow as sample enters fully developed plastic flow
- The small cube started around 6% error and continued to grow as simulation progressed
- Differences in responses was largely driven by differences in crystallographic texture
 - Follows historical trends already observed



Orientation distribution plots of large, medium, and small cube



Macroscopic stress strain curves for different size microstructures

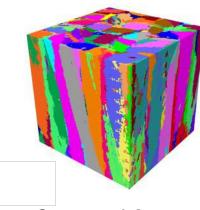


A Need for Mesh Coarsening

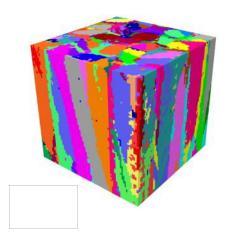
- Cellular Automata simulations produce microstructures with fine voxel sizes (1.667 microns)
 - Results in large number of elements for our simulations
 - 500³ micron sample had 27 million elements
 - Similar issues could come from either near-field high energy x-ray diffraction (nf-HEXD) or 3D-serial sectioned EBSD mapped microstructures
- Coarsening voxel data set reduces this issue
 - But what effects does this have on property calculations and intragrain heterogeneity responses?
- We're examining four levels of coarsening
 - Coarsen large microstructure 2, 3, 4, and 6 levels
 - Levels refer here to number of neighbor voxels averaged into 1 voxel in coarser mesh



Original Microstructure



Coarsen L2 Microstructure



Coarsen L4
Microstructure

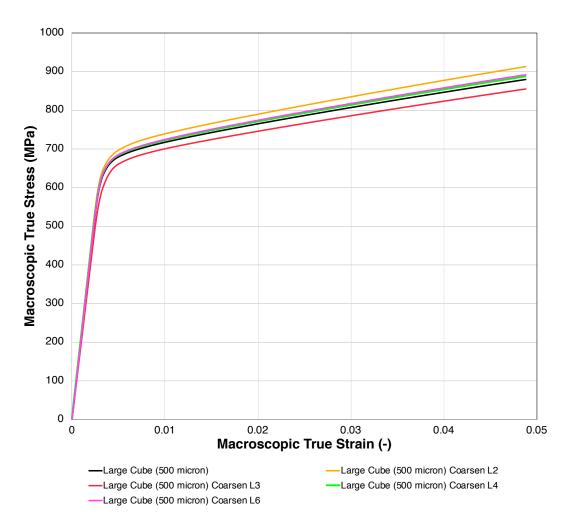


Coarsen L6 Microstructure



Macroscopic Stress-Strain Response

- Uniaxial tension tests out to 5% were taken on these samples
 - Symmetry boundary conditions were applied to all samples
- Stress-strain responses differed by at most 3% from the original mesh for all cases
- Crystallographic texture driving similarities in response
 - Voce hardening model lacks size dependence which could affect the trends seen here

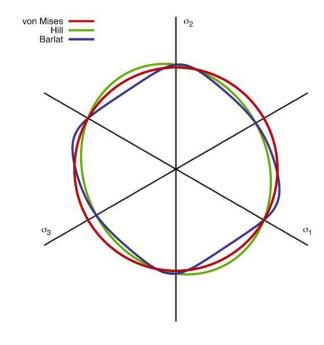


Macroscopic stress strain curves for different size microstructures



Why an anisotropic yield surface?

- If you're dealing with a strongly textured material a J2-type model probably isn't going to cut it
 - Rolling process to create sheet metal is well known for creating a textured materials that have orthotropic like behavior
- As-built AM materials can develop strong textures in the build direction
 - Post-build heat treatments and manufacturing processes such as HIP (high isostatic pressure) can reduce this issue
- Examine how varying the anisotropic properties of the material affects desired performance of a part



Yield surface comparison in the π -plane for 2090-T4 Al parameterization given in [9,10]



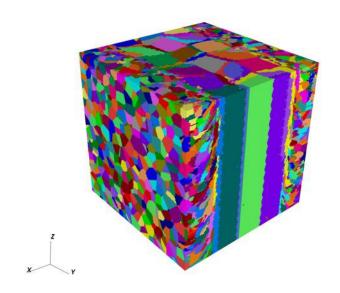
Barlat Yield Surface Model (Yld2004-18p)

- Barlat and his associates have created several yield surfaces over the year to improve modelling of manufacturing processes
 - Sheet metal processes was one of the largest drivers in this process
- The Yld2004-18p model is one of his more famous ones
 - 18 parameter model that's largely orthotropic with some out of plane behavior
 - Nice properties in that it can reduce to several famous models such as J2, Hill, and Tresca yield surface model
 - As of end of 2021, we have this implemented in one of LLNL's inhouse material library
 - An open-source version will be coming to ExaCMech within a year or so

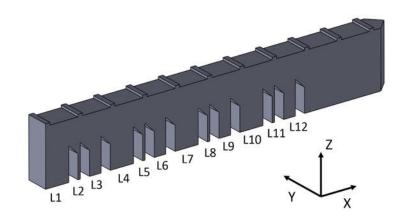


Implementation into an AM workflow

- Barlat model has traditionally been parameterized using experimental data
 - Data is not always easy to obtain nor cheap but simulations are "cheap"
 - Crystal plasticity simulations to the rescue
- ExaConstit is going to drive our simulations along with some workflow tools and python
 - Workflow tools will eventually be released as part of ExaConstit repo (contact if interested in them)
- Microstructure provided by an outside code, ExaCA
- Simple SciPy optimization function used to reduce error between the yield function predicted by Barlat model and outputted simulation response
 - Certain load conditions also make use of r-factor



Microstructure of interest (L8 leg down below*)





We are collaborating with the ExaWorks team to enable execution of ExaAM workflow on Exascale platforms.

• Flux-based implementation of ExaCA-ExaConstit workflow resulted in a 2x improvement

Simulations Preprocessing Postprocessing Python script Python script ExaConstit 1) Read in ExaCA output file 2) Associate grain number to each 1) Read in all macroscopic 1) Read in test matrix CA voxel stress-strain curves and 2) Edit option file for simulation 3) Relate grain to orientation data total plastic work per 4) Create a unique orientation set parameters across all grains (BCs, property file, mesh temperature 5) Renumber grains 2) Optimize Yld2004-18p file, time steps, ...) 6) Output text file with grain IDs for parameters to yield 3) Generate test directories each voxel stress values and job scripts using either 7) Output orientation file for each 3) Repeat step 1 for Flux or LSF grain different temperatures 4) Run all simulations 8) mesh generator reads in grain 4) Feed parameters into ID file and outputs an mfem mesh macroscopic part scale Looking at 21 simulations per 9) Generate test matrix RVE/mesh at a given temperature model (BCs, property file, mesh file, (63 simulations per RVE across all time steps, ...) temperature ranges)



Preprocessing Step

- Python CLI script takes in a microstructure, generates a mesh, and creates a test matrix
 - Provided multiple temperatures and their corresponding property files
 - Can coarsen microstructure if needed
 - Test matrix generated will be later slurped up by job generation script

```
python3 ./exaconstit_cli_preprocessing.py -ifdir ./ -ifile exaca.csv -ofdir ./output_dir/ -runame
super_cool_microstructure -c 1 -mg -mgdir ./ -t 298.0 -fprops ./props_cp_voce_in625.txt -nprops 17 -fstate
./state_cp_voce.txt -nstates 24
```

```
if (args.mesh_generator):
    with cd(fdiro):
        result = subprocess.run('pwd', stdout=subprocess.PIPE)
        pwd = result.stdout.decode('utf-8')

with cd(args.mesh_generator_dir):
    cmd = './mesh_generator'
    args = '-nx ' + str(dnx) + '-ny ' + str(dny) + '-nz ' + str(dnx)
    args = args + '-lx ' + str(lx) + '-ly ' + str(ly) + '-lz ' + str(lz)
    args = args + '-grain ' + pwd.strip() + '/' + gr_out
    args = args + '-or ' + pwd.strip() + '/' + fout + '.mesh'
    args = args + '-ord 1 -auto_mesh'
    cmd = cmd + ' ' + args
    print(cmd)
    result = subprocess.run(cmd, stdout=subprocess.PIPE, shell=True)
    mesh_file_loc = pwd.strip() + '/' + fout + '.mesh'
```

Test matrix creation

Mesh generation code



Job Generation Step

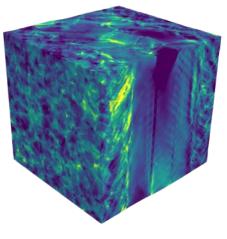
- Python CLI script takes in a test matrix, master option file, and a job submission file
 - Each simulation gets a unique job directory that has symlinks to original shared data
 - Master option file has regex searchable expressions in it that are replaced with test matrix values
 - Supports LSF or Flux job submission systems
 - Flux only required an additional 5 lines of code...
 - Generates a master job script that will submit all jobs for you
- Job generation could easily be extended to parametric studies

```
python3 ./job_cli.py -sdir ./ -odir ./../workflow_runs/ -
imtfile options_master.toml -iotfile options.toml -ijfile
hip_mechanics.flux -ijfd ./ -iofile options.csv
```

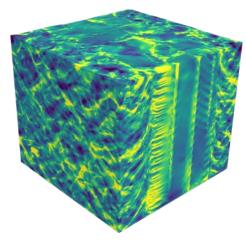
```
EXASCALE COMPUTING PROJECT
```

```
for iDir in range(nruns):
    rve_name = df["rve_unique_name"][iDir]
   load_dir_name = df["loading_name"][iDir]
   temp_k = str(int(df["tempk"][iDir]))
   fdiron = os.path.join(fdiro, rve_name, "")
   fdironl = os.path.join(fdiron, load_dir_name+"_"+temp_k, "")
   if not os.path.exists(fdironl):
        os.makedirs(fdironl)
   # Create symlink
   for src in glob.glob(os.path.join(fdirs,"*")):
        fh = os.path.join(fdironl, os.path.basename(src))
       if not os.path.exists(fh):
            os.symlink(src, fh)
   for iheader in headers:
        search = "%%" + iheader + "%%"
        repl val = str(df[iheader][iDir])
       # This line is needed as toml parsers might get mad with just the
       # 0. and not 0.0
        repl val = fixEssVals(repl val)
        toml = re.sub(search, repl_val, toml)
   # Now do the avg_stress, avg_pl_work, avg_dp_tensor replacements
   # We always want these to be unique names so if they're moved somewhere
   # else we can always associate them with the correct run
   # therefore, the name contains the rve name, temperature, and loading dir name
   # frve_name+"_"+str(temp)+"_"+loading_dir_names[0]
   ext_name = rve_name +"_" + temp_k + "_" + load_dir_name
   for iheader in avg_headers:
        search = "%%" + iheader + "%%"
        replace = ext_name
        toml = re.sub(search, replace, toml)
   # Output toml file
   fh = os.path.join(fdironl, os.path.basename(fotoml))
   # Check to see if it is a symlink and if so remove the link
   if os.path.islink(fh):
        os.unlink(fh)
   # We can now safely write out the file
   with open(fh, "w") as f:
        f.write(toml)
   # Output job script file
   fh = os.path.join(fdironl, os.path.basename(fin))
   # Check to see if it is a symlink and if so remove the link
   if os.path.islink(fh):
        os.unlink(fh)
   # We can now safely write out the file
   with open(fh, "w") as f:
        f.writelines(job_script)
   os.chmod(fh, 00775)
```

(Aside) AM microstructures have some crazy heterogeneous deformation

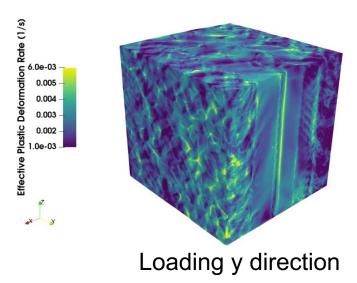


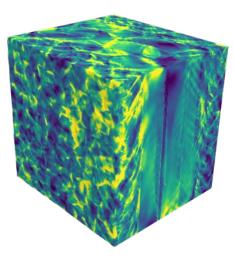
Loading x direction



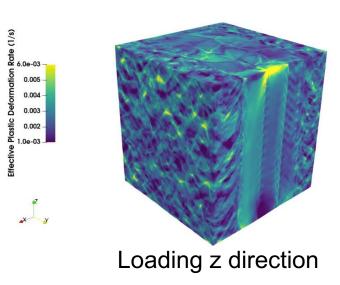
Equal biaxial loading x-y direction

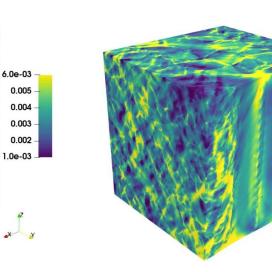






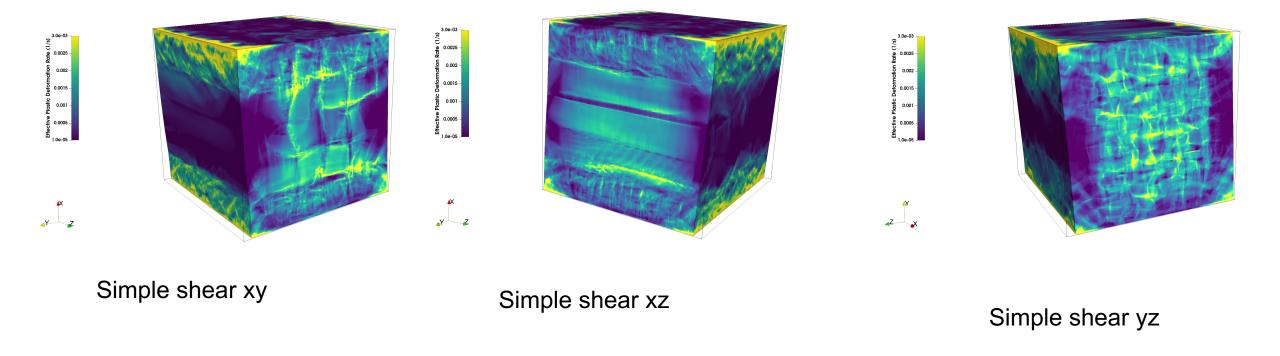
Equal biaxial loading y-z direction





Equal biaxial loading x-z direction

(Aside) AM microstructures have some crazy heterogeneous deformation





Optimization Procedure

- For each temperature load up all volume average stress-strain responses and total volume plastic work values
 - Loading in the build direction (z-axis) is considered ground-truth for optimization purposes
 - Calculate 0.2% off-set yield and the plastic work associated with that
 - For all simulations find strain step closest to plastic work produce above and use associated stress value to calculate von Mises stress to be used in optimization procedure
 - Let optimization function do its thing (go grab some coffee/do other work)
 - Later temperatures use previous temperature parameters as initial guess to get within ball park



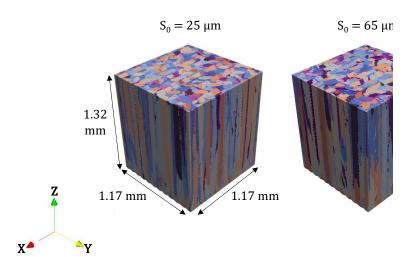
ExaConstit in other areas

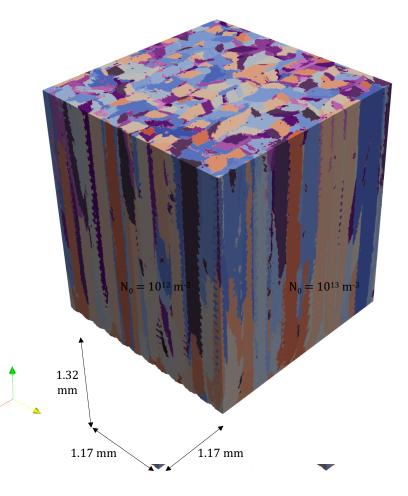
- ExaConstit can be used in areas outside of just the AM field
 - Quantifying variability in microstructure effects on material response
 - Fatigue applications and understanding deformation mechanisms at micro-scale is a large research area
 - Creating better material models to capture single crystal behavior
 - Modelling geological materials to understand how Earth's lower mantle deforms
 - Coupling experiments and simulations by using forward diffraction techniques
 - Modelling texture evolution of materials over large deformations



Variability in processing conditions and effects on mechanical response

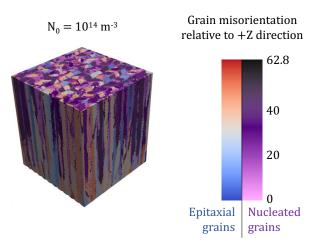
- Varying processing conditions mechanical response of a material
 - Wide parameter space so usu
- ExaAM team conducted a stugeneration code, and effects c





n effect the micro-

ExaCA, microstructure es

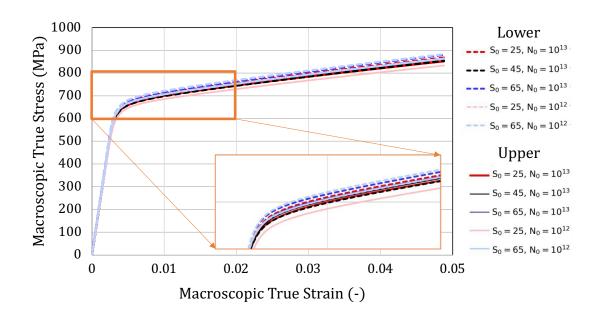






Variability in processing conditions and effects on mechanical response

- Varying the substrate diameter and nucleation rate does affect the macroscopic response of the material
 - In cases examined, a difference of ~6% was noted between the min and max stress-strain responses
- Variation within the intragrain response was also noted and a larger variability was noted here as well

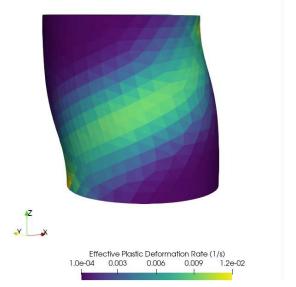


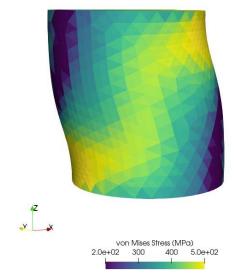
Variation of AM substrate diameter and nucleation rate effects on macroscopic response

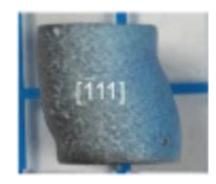


Simulating single crystal responses

- Capturing single crystal response of metals is often challenging as traditional crystal plasticity models were designed to capture response of polycrystalline materials
- We have an LDRD set-up to better examine this area and our working on some promising new model formulations
 - Capture buckling behavior as seen in experimental results as well as stress-strain response









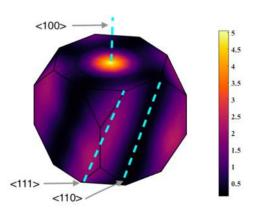
Crystallographic Texture Evolution

- Crystallographic texture informs of us the orientation dependence of a part in a given direction
- Texture plays a large role in determining how a part will deforms
- Manufacturers use texture to their advantage
 - Gas turbine blades are oriented in the <100> direction to improve fatigue life [11]
 - Accounting for texture allows deep forming operations to reduce waste [12]
- Large texture development occurs over large applied strains
 - ExaAM is not concerned with strains typically needed for texture development

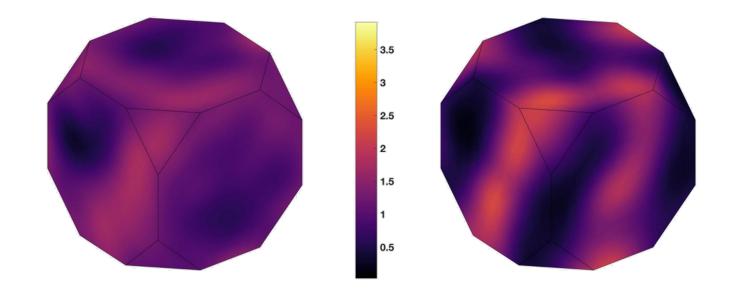


Crystallographic Texture Evolution of AM parts

 A CA microstructure sample was monotonically compressed to 30% strain in order to develop a strong texture in the <110> direction



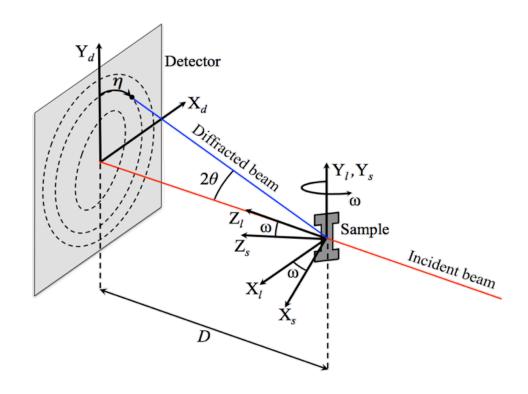
Example of strongly textured material with various fibers labelled [13]



Initial (Left) and final (Right) crystallographic texture of the CA sample



Simulating High Energy X-ray Diffraction Experiments



The peak data includes information about strain and lattice orientation of a grain



Simulating High Energy X-ray Diffraction Experiments

- Peak data is integrated in ω direction and either θ or η direction
 - Provides us with info about relative amounts of intragrain heterogeneity in either orientation, η spread, or strain, θ spread.

- Provides direct comparison to experiments

Fit 2θ Points

Fit η Points

Fit η Points

Fit η Points

Azimuth

FWHM

Spread in peak data tells us relative amounts of intragrain heterogeneity in the elastic deformation



Summary

- ExaConstit is an open-source crystal-plasticity FEM code built on MFEM
 - Highly performant on systems ranging from desktops all the way to systems such as Summit
 - Implemented several different integrators for GPU support and different materials models
- Created a workflow in-collaboration with ExaWorks team to efficiently run large number of simulations needed to calculate local properties used in ExaAM's part scale simulations
 - Led to anisotropic yield surface model being added to one of LLNL's material modelling libraries
- ExaConstit is well poised to tackle a wide range of research topics within the crystal plasticity community



Questions?



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